

# Resource Allocation for a Massive MIMO Relay Aided Secure Communication

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**Abstract**—In this paper, we address the problem of joint power and time allocation for secure communications in a decode-and-forward massive multiple-input multiple-output (M-MIMO) relaying system in the presence of a passive eavesdropper. We apply the M-MIMO relaying technique to enhance the secrecy performance under very practical and adverse conditions, i.e., no availability of instantaneous eavesdropper channel state information (CSI) and only imperfect instantaneous legitimate CSI. We first provide a performance analysis of secrecy outage capacity, which reveals the minimum required number of relay antennas for achieving a positive secrecy outage capacity. Then, we propose an optimization framework to jointly optimize source transmit power, relay transmit power, and transmission time in each hop, with the goal of maximizing the secrecy outage capacity. Although the secrecy outage capacity is not a concave function with respect to the optimization variables, we show that it can be maximized by first maximizing over some of the variables, and then maximizing over the rest. To this end, we first derive a closed-form solution of optimal relay transmit power, afterward obtain that of optimal source transmit power, and then derive the optimal ratio of the first-hop duration to a complete transmission time. Moreover, several important system design insights are provided through asymptotic performance analysis. Finally, simulation results validate the effectiveness of the proposed joint resource allocation scheme.

**Index Terms**—Physical layer security, massive MIMO, DF relaying protocol, resource allocation.

## I. INTRODUCTION

SECURE communication over wireless channels is always a critical issue due to the broadcast nature of the wireless medium. Traditionally, secure communication is guaranteed by high-layer encryption [1]. However, the secrecy provided by

the commonly used encryption technique is threatened by the rapid development of the computing devices, such as quantum computers. Additionally, the encryption technique requires a secure channel for the exchange of a private key, which may be impractical in mobile and ad-hoc wireless networks. Inspired by seminal works of Shannon [2] and Wyner [3], it is found that perfectly secure communication can be realized only by exploiting physical layer techniques, namely physical layer security (PHY-security). The crux of physical layer security is to exploit the physical characteristics of wireless channels, i.e., fading, noise and interference, so as to maximize the rate difference between the main channel and the wiretap channel, namely secrecy rate [4]–[6].

Wyner showed that when the eavesdropper channel is a degraded version of the legitimate channel, an achievable positive secrecy rate exists. However, the feasibility of PHY-security in traditional single-antenna systems may be hampered by channel condition. For instance, if the eavesdropper channel is more capable than the legitimate channel, a zero secrecy rate might result [7]. In contrast, multiple-antenna system can handle the secrecy problem in communication networks more efficiently via spatial beamforming, which has been confirmed by extensive researches [8]–[12] and references therein. The authors in [13] characterized the optimal spatial beamformer in terms of a generalized eigenvector for a point-to-point multiple-antenna system where the transmitter and the eavesdropper are equipped with multiple antennas and the intended receiver has a single antenna. Furthermore, in the case of a multiple-antenna eavesdropper, a computable characterization of the spatial beamformer was established as the saddle point solution to a minimax problem in multiple-input multiple-output (MIMO) wiretap channel in [14]. It is shown that multiple-antenna techniques can effectively improve the secrecy rate by exploiting spatial degrees of freedom. Moreover, as an important security-enhancing technique, cooperative relaying has also received considerable attention [15]–[17]. The authors in [18] provided a detailed analysis of various secure cooperative schemes, i.e., decode-and-forward (DF), amplify-and-forward (AF), and cooperative jamming (CJ), for a relay aided communication system in the presence of one or more eavesdroppers. The use of a relay might shorten the communication distance, and thus improve the secrecy rate. Besides, the relay can confuse the eavesdropper by sending artificial noise (AN) for assisting the secure transmission from the source to the legitimate destination [19].

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To further improve the secrecy performance, multiple-antenna techniques and cooperative relaying techniques can be combined in secure communication systems [20]. In [21] and [22], optimal beamforming schemes for a multiple-antenna relay in two-hop secure communications based on AF and DF relaying protocols were presented, respectively. It is worth pointing out that the optimal beamforming schemes rely on the perfect knowledge of both the legitimate channel and the eavesdropper channel. However, in practice, the instantaneous eavesdropper CSI may be imperfect or even unavailable, since the eavesdropper is usually passive and well hidden. Therefore, robust secure beamforming combined with AN was proposed to maximize the worst-case secrecy rate in presence of imperfect eavesdropper CSI [23]. Furthermore, if there is no instantaneous eavesdropper channel state information (CSI), a joint beamforming and jamming scheme can be employed according to [24]. Specifically, the AN is transmitted in the null space of the legitimate channel, so as to confuse the eavesdropper while avoiding interference to the legitimate destination [25], [26]. In practice, instantaneous legitimate CSI at the transmitter is often imperfect due to channel estimation errors or limited CSI feedback [27]. In this case, the AN will also interfere with the legitimate signal resulting in a loss of secrecy rate. Thus, it is necessary to introduce new MIMO relaying techniques to effectively enhance wireless security under very practical and adverse assumptions, i.e., no instantaneous eavesdropper CSI and imperfect instantaneous legitimate CSI. Recently, it is found that massive MIMO (M-MIMO) can produce high-resolution spatial beams, and thus information leakage to an unintended user is expected to be negligible [28]–[30]. In [31] and [32], M-MIMO techniques were applied to secure relaying systems without instantaneous eavesdropper CSI and with imperfect instantaneous legitimate CSI. It was shown that even in a very adverse environment, such as short-distance interception, the secrecy performance can be improved significantly by M-MIMO techniques.

To guarantee secure relaying communications, there are a variety of available physical layer resources, i.e., antenna, time, and power. Through resource allocation, it is expected that the secrecy performance can be further improved [33]. However, resource allocation in secure relaying communications might affect the signal quality at both the legitimate destination and the eavesdropper. Thus, it is not a trivial task to carry out optimal resource allocation. In [34], the transmit powers at the source and the relay were jointly optimized, so as to maximize the secrecy outage capacity in DF secure relay networks without instantaneous eavesdropper CSI and with imperfect instantaneous legitimate CSI. Moreover, for secure relaying systems, it is necessary to allocate time between the first and the second hops optimally for a given duration of a complete transmission from the source to the destination. Considering cooperative relaying in secure cognitive radio networks, the optimal joint time and power allocation was derived in [35] for maximizing the secrecy rate. In [36], optimal relay power allocation schemes were proposed in DF M-MIMO secure relaying systems for maximizing the secrecy outage capacity and minimizing the

interception probability, respectively. To the best of authors' knowledge, joint time and power allocation in DF M-MIMO secure relaying systems under practical conditions is still an open issue. In this paper, we focus on the analysis and design of a joint time and power allocation scheme for a DF M-MIMO secure relaying system in the sense of maximizing the secrecy outage capacity. The contributions of this paper are as follows:

- 1) We provide a performance analysis in terms of secrecy outage capacity for a DF M-MIMO secure relaying system without instantaneous eavesdropper CSI and under imperfect instantaneous legitimate CSI. Our results reveal the requirement on the minimum number of relay antennas for achieving a positive secrecy outage capacity.
- 2) We propose a joint source transmit power, relay transmit power, and time allocation scheme through maximizing the secrecy outage capacity. We obtain closed-form solutions of optimal power allocation at the source and the relay, and derive the optimal time allocation for the two-hop communication by using the Lagrange multiplier method. Simulation results show that the proposed scheme can achieve the same performance as the optimal resource allocation scheme based on a three-dimensional exhaustive search, and has a significant performance gain over fixed resource allocation schemes.
- 3) We find that full power transmission at the source is always optimal for maximizing the secrecy outage capacity, despite the non-convexity of the considered problem. Moreover, given a maximum transmit power constraint at the relay, the secrecy outage capacity is saturated when the maximum available source power is sufficiently large. Similarly, for a given maximum power constraint at the source, the secrecy outage capacity is also saturated as the maximum available relay power increases.

The remainder of this paper is organized as follows. A two-hop DF M-MIMO secure relaying system model is introduced in Section II. In Section III, we propose a joint power and time allocation scheme for maximizing the secrecy outage capacity. In Section IV, we present some simulation results to validate the effectiveness of the proposed scheme. Finally, we conclude the paper in Section V.

*Notation:* Bold upper (or lower) case letters are used to denote matrices (or column vectors),  $(\cdot)^H$  is to denote conjugate transpose,  $E[\cdot]$  is used to denote expectation,  $\|\cdot\|$  is to denote the  $L_2$  norm of a vector,  $|\cdot|$  denotes the absolute value,  $(a)^+$  denotes the operation  $\max(a, 0)$ ,  $f'(x)$  and  $f''(x)$  denote the first and second derivative of  $f(x)$  with respect to  $x$ , and  $\sim$  is used to denote the equality in distribution. The acronym "i.i.d." means "independent and identically distributed", "pdf" means "probability density function", and "cdf" stands for "cumulative distribution function".

## II. SYSTEM MODEL

We consider a device-to-device (D2D) communication over a relay in Beyond 4th Generation (B4G) systems, as depicted in Fig. 1. A source sends a message to a legitimate destination with the aid of a relay, while an eavesdropper intends to intercept the message. We assume that the relay is fixed

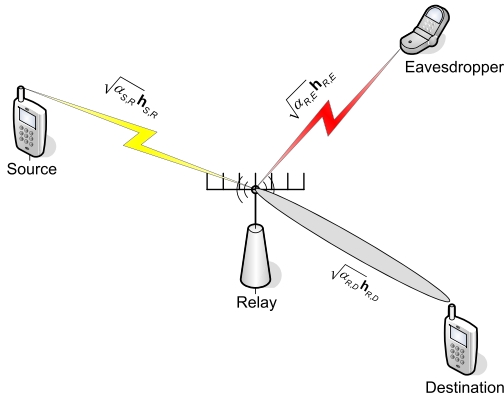


Fig. 1. A DF M-MIMO secure relaying system.

and equipped with a massive antenna array, which is a key technology in B4G systems. According to [37], a massive antenna array in B4G systems typically will comprise  $N_R \geq 64$  antennas. The other nodes are equipped with a single antenna each due to the size limitation of mobile devices. Besides, the eavesdropper may be an idle destination or pretends to be a legitimate receiver, such that it also employs a single antenna. Due to a long propagation distance, the direct transmission from the source to the legitimate destination does not exist. The relay works in a half-duplex mode, which means a complete transmission requires two orthogonal time slots. Specifically, the source sends the signal to the relay in the first time slot, and then the relay forwards the decoded signal to the legitimate destination in the second time slot. In this paper, it is assumed that the time duration of a two-hop transmission is  $T$  fixedly, and the transmission duration of the first hop is  $\theta T$  with  $0 < \theta < 1$ . In practice, the relay is far away from the source, such that it is difficult for the single-antenna eavesdropper to overhear both the source and the relay due to a long distance. Moreover, if the eavesdropper is an idle destination, it is close to the relay, but not to the source. Thus, following the previous related works [16], [38], we also assume that the eavesdropper only monitors the transmission from the relay to the destination.

We use  $\sqrt{\alpha_{S,R}}\mathbf{h}_{S,R}$ ,  $\sqrt{\alpha_{R,D}}\mathbf{h}_{R,D}$ , and  $\sqrt{\alpha_{R,E}}\mathbf{h}_{R,E}$  to represent the channels from the source to the relay, the relay to the destination, and the relay to the eavesdropper respectively, where  $\alpha_{S,R}$ ,  $\alpha_{R,D}$ , and  $\alpha_{R,E}$  are the distance-dependent path losses, and  $\mathbf{h}_{S,R}$ ,  $\mathbf{h}_{R,D}$ , and  $\mathbf{h}_{R,E}$  are  $N_R$ -dimensional channel small-scale fading vectors with independent and identically distributed (i.i.d.) zero mean and unit variance complex Gaussian entries. It is assumed that the channels remain constant during a time slot  $T$  and change independently over slots. Thus, the received signal at the relay in the first time slot can be expressed as

$$\mathbf{y}_R = \sqrt{P_S \alpha_{S,R}} \mathbf{h}_{S,R} s + \mathbf{n}_R, \quad (1)$$

where  $s$  is the Gaussian distributed transmit signal with a unit power,  $P_S$  is the transmit power at the source, and  $\mathbf{n}_R$  is the additive white Gaussian noise (AWGN) vector with covariance matrix  $\mathbf{I}_{N_R}$  at the relay. We assume that the relay has perfect

instantaneous CSI about  $\mathbf{h}_{S,R}$  through channel estimation based on pilots. Since maximum ratio combining (MRC) can achieve an asymptotically optimal performance in M-MIMO systems with a low complexity [39], the relay employs this reception scheme to recover the information from the source. Thus, the received signal after MRC becomes

$$\hat{y}_R = \sqrt{P_S \alpha_{S,R}} \frac{\mathbf{h}_{S,R}^H}{\|\mathbf{h}_{S,R}\|} \mathbf{h}_{S,R} s + \frac{\mathbf{h}_{S,R}^H}{\|\mathbf{h}_{S,R}\|} \mathbf{n}_R. \quad (2)$$

During the second time slot, the relay forwards the re-encoded Gaussian distributed signal  $\hat{s}$  of unit norm using maximum ratio transmission (MRT) due to its low complexity and good performance in M-MIMO systems. We assume that the relay only has partial CSI about  $\mathbf{h}_{R,D}$ . This is because the estimation of  $\mathbf{h}_{R,D}$  is commonly performed by making use of channel reciprocity in time division duplex (TDD) systems. However, due to duplexing and decoding delay, the resulting estimated CSI at the relay is usually imperfect [40]. In this case, the relation between the estimated CSI  $\hat{\mathbf{h}}_{R,D}$  and the actual CSI  $\mathbf{h}_{R,D}$  is given by

$$\mathbf{h}_{R,D} = \sqrt{\rho} \hat{\mathbf{h}}_{R,D} + \sqrt{1-\rho} \mathbf{e}, \quad (3)$$

where  $\mathbf{e}$  is the error noise vector with i.i.d., zero mean, and unit variance complex Gaussian entries, and is independent of  $\hat{\mathbf{h}}_{R,D}$ .  $0 \leq \rho \leq 1$  is the correlation coefficient between  $\hat{\mathbf{h}}_{R,D}$  and  $\mathbf{h}_{R,D}$ , which depends on delay duration and velocity of the destination [40]. Thus, the received signals at the destination and the eavesdropper are given by

$$\mathbf{y}_D = \sqrt{P_R \alpha_{R,D}} \mathbf{h}_{R,D}^H \mathbf{r} + n_D, \quad (4)$$

and

$$\mathbf{y}_E = \sqrt{P_R \alpha_{R,E}} \mathbf{h}_{R,E}^H \mathbf{r} + n_E, \quad (5)$$

respectively, where  $P_R$  is the transmit power of the relay, and  $\mathbf{r} = \mathbf{v}_R \hat{s}$  is the forwarded signal with  $\mathbf{v}_R = \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|}$  being an MRT beamformer.  $n_D$  and  $n_E$  are AWGNs with unit variance at the destination and the eavesdropper, respectively.

Since the eavesdropper is usually passive and keeps silent, instantaneous CSI about  $\mathbf{h}_{R,E}$  is unavailable at the relay. In this paper, we assume that the relay only has statistical knowledge about the channel from the relay to the eavesdropper, such as  $\alpha_{R,E}$ . This is reasonable because if the eavesdropper is an idle destination, the relay may obtain the position information. In the case of no instantaneous eavesdropper CSI, it is impossible to guarantee that the selected transmission rate is not greater than the secrecy capacity over fading channels. To evaluate the wireless security, we adopt secrecy outage capacity as a performance metric, which is defined as the maximum transmission rate such that the probability that the selected transmission rate is greater than the secrecy capacity is smaller than a given value [41]. Mathematically, it can be obtained from the condition

$$P_r(R_{soc} > C_D - C_E) = \varepsilon, \quad (6)$$

where  $C_D$  and  $C_E$  are the legitimate and eavesdropper channel capacities, respectively.  $\varepsilon$  is the maximum tolerable outage probability associated to a secrecy outage capacity  $R_{soc}$ .

### III. JOINT POWER AND TIME ALLOCATION

In this section, we first analyze the secrecy outage capacity for the considered DF M-MIMO secure relaying system under the situation of no instantaneous eavesdropper CSI and imperfect instantaneous legitimate CSI. Then, we reveal the condition for achieving a positive secrecy outage capacity. Finally, we propose a joint power and time allocation scheme for maximizing the secrecy outage capacity.

#### A. Some Primary Results on Very Long Random Vectors

In this paper, we consider a M-MIMO relaying system, and thus the channels can be modeled by very long random vectors. During the analysis, we will use some primary results on very long random vectors. Prior to performance analysis, we first introduce these useful results.

Let  $\mathbf{p} \triangleq [p_1 \dots p_n]^T$  and  $\mathbf{q} \triangleq [q_1 \dots q_n]^T$  be mutually independent  $n \times 1$  vectors whose elements are i.i.d. zero mean random variables with variances  $\sigma_p^2$  and  $\sigma_q^2$ , respectively. Then, as  $n \rightarrow \infty$ , the very long random vectors  $\mathbf{p}$  and  $\mathbf{q}$  have the following properties [42]:

A: According to the law of large numbers, we have

$$\frac{1}{n} \mathbf{p}^H \mathbf{p} \xrightarrow{a.s.} \sigma_p^2, \quad (7)$$

where  $\xrightarrow{a.s.}$  denotes the almost sure convergence.

B: According to the Lindeberg-Lévy central limit theorem, we have

$$\frac{1}{\sqrt{n}} \mathbf{p}^H \mathbf{q} \xrightarrow{d} \mathcal{CN}(0, \sigma_p^2 \sigma_q^2), \quad (8)$$

where  $\xrightarrow{d.}$  denotes convergence in distribution.

#### B. Secrecy Outage Capacity

In this section, we focus on the analysis of secrecy outage capacity in the considered DF M-MIMO secure relaying system. Based on the received signal after performing MRC at the relay in (2), the channel capacity between the source to the relay can be written as

$$C_{S,R} = \theta \log_2(1 + \gamma_R), \quad (9)$$

where  $\gamma_R = P_S \alpha_{S,R} \|\mathbf{h}_{S,R}\|^2$  is the received signal-to-noise ratio (SNR) at the relay. Similarly, according to (4) and (5), channel capacities from the relay to the destination and from the relay and the eavesdropper are given by

$$C_{R,D} = (1 - \theta) \log_2(1 + \gamma_D), \quad (10)$$

and

$$C_{R,E} = (1 - \theta) \log_2(1 + \gamma_E), \quad (11)$$

respectively, where  $\gamma_D = P_R \alpha_{R,D} \left| \mathbf{h}_{R,D}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2$  and  $\gamma_E = P_R \alpha_{R,E} \left| \mathbf{h}_{R,E}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2$  are SNRs at the destination and the eavesdropper, respectively.

According to the property of a two-hop DF relaying system, the legitimate and the eavesdropper channel capacities can be computed as

$$C_D = \min(C_{S,R}, C_{R,D}), \quad (12)$$

and

$$C_E = \min(C_{S,R}, C_{R,E}), \quad (13)$$

respectively.

Then, for the secrecy outage capacity in such a DF M-MIMO secure relaying system without instantaneous eavesdropper CSI and with imperfect instantaneous legitimate CSI, we have the following theorem:

*Theorem 1:* Given a maximum tolerable outage probability  $\varepsilon$ , the secrecy outage capacity can be tightly approximated as  $R_{soc}(P_R, P_S, \theta) = \min(\theta \log_2(1 + P_S \alpha_{S,R} N_R), (1 - \theta) \log_2(1 + P_R \alpha_{R,D} \rho N_R) - (1 - \theta) \log_2(1 - P_R \alpha_{R,E} \ln \varepsilon))$ , if the number of relay antennas is sufficiently large.

*Proof:* Please refer to Appendix A.  $\blacksquare$

From Theorem 1, it is known that the secrecy outage capacity is an increasing function of the number of relay antennas for a given outage probability requirement. Thus, it is possible to improve the secrecy outage capacity by adding relay antennas. In the sequel, we further analyze the effect of  $N_R$  on the secrecy performance. For notational simplicity, we let  $\alpha_{S,R} N_R = A$ ,  $\alpha_{R,D} \rho N_R = B$ ,  $-\alpha_{R,E} \ln \varepsilon = B \cdot r_l$ , where  $r_l = -\frac{\alpha_{R,E} \ln \varepsilon}{\alpha_{R,D} \rho N_R}$ . Then, the secrecy outage capacity can be rewritten as (14), as shown at the bottom of this page.

Note that the secrecy outage capacity may be negative from a pure mathematical view. Now, we find the condition for achieving a positive secrecy outage capacity. Observing the above secrecy outage capacity, we get the following proposition:

*Proposition 1:* Only if  $0 < r_l < 1$ , the secrecy outage capacity in such a DF M-MIMO secure relaying system in presence of imperfect CSI is positive.

*Proof:* Please refer to Appendix B.  $\blacksquare$

From Proposition 1, it is known that if  $r_l \geq 1$ , the positive secrecy outage capacity does not exist despite the values of  $P_R$ ,  $P_S$ , and  $\theta$ . Thus,  $0 < r_l < 1$  is the premise for power and time allocation in the considered DF M-MIMO secure relaying system. Given channel conditions and a secrecy outage probability requirement, there exists a minimum required number of antennas at the relay in order to fulfill the condition  $0 < r_l < 1$ . Then, we have the following proposition:

*Proposition 2:* In order to achieve a positive secrecy outage capacity, the number of antennas at the relay,  $N_R$ , must be larger than  $-\frac{\alpha_{R,E} \ln \varepsilon}{\rho \alpha_{R,D}}$ .

$$R_{soc}(P_R, P_S, \theta) = \begin{cases} (1 - \theta) \log_2(1 + P_R B) - (1 - \theta) \log_2(1 + P_R B r_l), & P_R \leq \frac{(1 + P_S A)^{\frac{\theta}{1-\theta}} - 1}{B} \\ \theta \log_2(1 + P_S A) - (1 - \theta) \log_2(1 + P_R B r_l), & P_R \geq \frac{(1 + P_S A)^{\frac{\theta}{1-\theta}} - 1}{B} \end{cases} \quad (14)$$

*Proof:* According to the definition of  $r_l = -\frac{\alpha_{R,E} \ln \varepsilon}{\rho \alpha_{R,D} N_R}$ ,  $0 < r_l < 1$  is equivalent to  $N_R > -\frac{\alpha_{R,E} \ln \varepsilon}{\rho \alpha_{R,D}}$ . ■

Note that the more stringent the secrecy outage probability requirement is, the large the required minimum number of relay antennas is. However, for any non-zero secrecy outage probability tolerance, i.e.,  $0 < r_l < 1$  can always satisfy by deploying more relay antennas, which is an advantage of the considered M-MIMO relaying system. As a result, in what follows, we only consider the case of  $0 < r_l < 1$  for the design of resource allocation.

### C. Joint Power and Time Allocation

Intuitively, both power and time are scarce and critical resources in wireless communication systems. Especially for secure communication, an inappropriate resource allocation may not only waste the resource, but may also degrade the secrecy performance. This is because resource allocation will affect the performance of both the legitimate channel and the eavesdropper channel simultaneously. Thus, it is necessary to jointly optimize power and time for maximizing the secrecy outage capacity.

In general, joint power and time allocation in the considered DF M-MIMO secure relaying system can be formulated as the following optimization problem:

$$J_1 : \max_{P_R, P_S, \theta} R_{soc}(P_R, P_S, \theta) \quad (15)$$

$$\text{s.t. } P_R \leq P_{R,\max} \quad (16)$$

$$P_S \leq P_{S,\max} \quad (17)$$

$$0 < \theta < 1, \quad (18)$$

where  $P_{S,\max}$  and  $P_{R,\max}$  are the maximum transmit power budgets at the source and the relay, respectively. Unfortunately, the objective function (15) in  $J_1$  is not a convex function with respect to  $P_S$ ,  $P_R$ , and  $\theta$ , and thus it is difficult to obtain the optimal solution directly. To address this challenging problem, we apply the following property  $\inf_{x,y} f(x,y) = \inf_x \tilde{f}(x)$ , where  $\tilde{f}(x) = \inf_y f(x,y)$  [43]. In other words, we can always minimize a function by first minimizing over some of the variables, and then minimizing over the remaining ones. This simple and general principle can be used to transform a difficult problem into solvable equivalent forms. Hence, to solve the non-convex optimization problem  $J_1$ , we can apply this principle twice. Specifically, we first maximize the objective function by maximizing over  $P_R$ , then over  $P_S$ , and finally solve an equivalent optimization problem related to  $\theta$ .

1) *Maximization Over  $P_R$ :* By using the property mentioned above, we first maximize the objective function in (15) over  $P_R$  for given  $P_S$  and  $\theta$ , which can be formulated as

$$H_1 : R_1(P_S, \theta) = \max_{P_R} R_{soc}(P_R, P_S, \theta) \\ \text{s.t. } P_R \leq P_{R,\max}. \quad (19)$$

In the sequel, we focus on getting a closed-form expression of optimal power at the relay,  $P_R^*$ , and the corresponding maximum value of the objective function  $R_1(P_R, \theta)$ . By solving the optimization problem  $H_1$ , we have the following theorem about the closed-form expression of  $P_R^*$  and  $R_1(P_S, \theta)$ :

*Theorem 2:* The optimal power at the relay is  $P_R^* = \min\left(\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}, P_{R,\max}\right)$ , and the corresponding maximum secrecy outage capacity is given by  $R_1(P_S, \theta) = (1-\theta) \log_2\left(1 + \min\left(\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}, P_{R,\max}\right) B\right) - (1-\theta) \log_2\left(1 + \min\left(\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}, P_{R,\max}\right) B r_l\right)$ .

*Proof:* Please refer to Appendix B. ■

*Remark:* It is found that if instantaneous eavesdropper CSI is unavailable, it is optimal for the DF secure relaying system to let the two hops have the same channel capacity, resulting in  $P_R^* = \min\left(\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}, P_{R,\max}\right)$ , see Appendix B. Moreover, it is proved that the optimal relay transmit power is an increasing function of source transmit power. Then, we can obtain the following proposition:

*Proposition 3:* If the maximum available source transmit power is sufficiently large, then the maximum secrecy outage capacity will be saturated with respect to source transmit power. The saturated secrecy outage capacity is upper bounded by  $R_1^{upper}(P_S, \theta) = (1-\theta) \log_2(1 + P_{R,\max} B) - (1-\theta) \log_2(1 + P_{R,\max} B r_l)$ , which is independent of  $P_S$  and is an increasing function of  $P_{R,\max}$ .

*Proof:* If  $P_{S,\max}$  is large enough, we always have  $P_R^* = \min\left(\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}, P_{R,\max}\right) = P_{R,\max}$ , which is a constant. In this case, the maximum secrecy outage capacity is independent of  $P_S$ , and the corresponding saturated value is equal to  $R_1^{upper}(P_S, \theta) = R_1(P_{R,\max}, \theta)$ . ■

2) *Maximization Over  $P_S$ :* Based on the Theorem 2, the optimization problem  $J_1$  is equivalent to

$$J_2 : \max_{P_S, \theta} R_1(P_S, \theta) \\ \text{s.t. } P_S \leq P_{S,\max} \\ 0 < \theta < 1. \quad (20)$$

Using the above mentioned property again, we first maximize the objective function in (20) over  $P_S$  for a given  $\theta$ . Thus, the optimization problem is transformed as

$$H_2 : R_2(\theta) = \max_{P_S} R_1(P_S, \theta) \\ \text{s.t. } P_S \leq P_{S,\max}. \quad (21)$$

By solving the above optimization problem, we get the following theorem:

*Theorem 3:* The optimal transmit power at the source from the perspectives of maximizing the secrecy outage capacity and minimizing the energy consumption is  $P_S^* = \min\left(P_{S,\max}, \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}\right)$ , and the corresponding maximum secrecy outage capacity is given by  $R_2(\theta) = \min\left((1-\theta) \log_2(1 + P_{R,\max} B) - (1-\theta) \log_2(1 + P_{R,\max} B r_l), \theta \log_2(1 + P_{S,\max} A) - (1-\theta) \log_2(1 + ((1 + P_{S,\max} A)^{\frac{\theta}{1-\theta}} - 1) r_l)\right)$ .

*Proof:* Please refer to Appendix C. ■

*Remark:* It is found that the optimal source transmit power at the source is not unique in the sense of maximizing the secrecy outage capacity. However,  $P_{S,\max}$  is always an optimal power. This is because increasing  $P_S$  does not degrade the secrecy performance since the eavesdropper only monitors the transmission from the relay to the destination. Then, from the perspective of reducing the computational complexity of the resource allocation algorithm, it is also likely to take  $P_{S,\max}$  as the optimal source transmit power. Similarly, for the case of a large relay transmit power constraint, we can get the following proposition:

*Proposition 4:* If the maximum available relay transmit power is sufficiently large, then the maximum secrecy outage capacity will be saturated with respect to relay transmit power. The saturated secrecy outage capacity is upper bounded by  $R_2^{upper}(\theta) = \theta \log_2(1 + P_{S,\max}A) - (1 - \theta) \log_2(1 + ((1 + P_{S,\max}A)^{\frac{\theta}{1-\theta}} - 1)r_l)$ , which is independent of  $P_R$ .

*Proof:* If  $P_{R,\max}$  is large enough, we always have  $P_S^* = \min\left(P_{S,\max}, \frac{(P_{R,\max}B+1)^{\frac{1-\theta}{\theta}} - 1}{A}\right) = P_{S,\max}$ , which is a constant. Thus, the maximum secrecy outage capacity is saturated, and the corresponding saturated value is  $R_2^{upper}(\theta) = \theta \log_2(1 + P_{S,\max}A) - (1 - \theta) \log_2(1 + ((1 + P_{S,\max}A)^{\frac{\theta}{1-\theta}} - 1)r_l)$ , which is independent of  $P_{R,\max}$ . ■

3) *Maximization Over  $\theta$ :* Based on Theorem 2 and 3, we transform the original problem  $J_1$  with three optimization variables  $P_S$ ,  $P_R$ , and  $\theta$  to a problem with only one optimization variable  $\theta$ , which is equivalent to  $J_3$  as below. Thus, we focus on getting an optimal solution of  $J_3$  in this subsection.

$$J_3 : \max_{\theta} R_2(\theta) \\ \text{s.t. } 0 < \theta < 1. \quad (22)$$

We first consider the case of  $\theta \geq \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1}$  or equivalently  $P_{S,\max} \geq \frac{(P_{R,\max}B+1)^{\frac{1-\theta}{\theta}} - 1}{A}$ . In this context, the objective function can be reduced as  $R_2(\theta) = \min\left((1 - \theta) \log_2(1 + P_{R,\max}B) - (1 - \theta) \log_2(1 + P_{R,\max}Br_l), \theta \log_2(1 + P_{S,\max}A) - (1 - \theta) \log_2(1 + ((1 + P_{S,\max}A)^{\frac{\theta}{1-\theta}} - 1)r_l)\right) = (1 - \theta) \log_2(1 + P_{R,\max}B) - (1 - \theta) \log_2(1 + P_{R,\max}Br_l)$ . Hence,  $J_3$  is simplified as  $G_1$  when  $\theta \geq \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1}$

$$G_1 : \max_{\theta} (1 - \theta) \log_2(1 + P_{R,\max}B) \\ - (1 - \theta) \log_2(1 + P_{R,\max}Br_l) \\ \text{s.t. } \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1} \leq \theta < 1. \quad (23)$$

Apparently,  $G_1$  is a decreasing function of  $\theta$ , thus it is easy to derive the optimal solution as  $\theta_1^* = \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1}$ , and

the corresponding maximum value of the objective function is  $\frac{\ln(P_{S,\max}A+1)}{\ln(P_{S,\max}A+1) + \ln(P_{R,\max}B+1)} \left( \log_2(1 + P_{R,\max}B) - \log_2(1 + P_{R,\max}Br_l) \right)$ .

Otherwise, if  $\theta \leq \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1}$  or equivalently  $P_{S,\max} \leq \frac{(P_{R,\max}B+1)^{\frac{1-\theta}{\theta}} - 1}{A}$ , the objective function in  $J_3$  is reduced as  $\theta \log_2(1 + P_{S,\max}A) - (1 - \theta) \log_2(1 + ((1 + P_{S,\max}A)^{\frac{\theta}{1-\theta}} - 1)r_l)$ . Therefore,  $J_3$  is equivalent to

$$G_2 : \max_{\theta} R_3(\theta) \quad (24)$$

$$\text{s.t. } \theta \leq \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1}, \quad (25)$$

where  $R_3(\theta) = \theta \log_2(1 + P_{S,\max}A) - (1 - \theta) \log_2(1 + ((1 + P_{S,\max}A)^{\frac{\theta}{1-\theta}} - 1)r_l)$ . Checking the convexity of  $R_3(\theta)$ , we have the following theorem:

*Lemma 1:* The objective function of  $G_2$ ,  $R_3(\theta)$ , is a concave function with respect to  $\theta$ , when  $\theta \leq \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1}$ .

*Proof:* Please refer to Appendix D. ■

According to the Lemma 1,  $G_2$  is a convex optimization problem, such that it can be solved by the Lagrange multiplier method. Therefore, we first construct the Lagrange dual function as follows

$$\mathcal{L}(\theta, \mu) = \theta W \log_2(1 + P_{S,\max}A) \\ - (1 - \theta) W \log_2(1 + ((1 + P_{S,\max}A)^{\frac{\theta}{1-\theta}} - 1)r_l) \\ - \mu \left( \theta - \frac{1}{\frac{\ln(P_{S,\max}A+1)}{\ln(P_{R,\max}B+1)} + 1} \right), \quad (26)$$

where  $\mu \geq 0$  is the Lagrange multiplier associated to the constraint (25). Hence, the dual problem of  $G_2$  is given by

$$\min_{\mu} \max_{\theta} \mathcal{L}(\theta, \mu). \quad (27)$$

For a given  $\mu$ , the optimal  $\theta$  can be derived by solving the following Karush-Kuhn-Tucker (KKT) condition [43]:

$$\frac{\partial \mathcal{L}(\theta, \mu)}{\partial \theta} = \frac{\partial R_3(\theta)}{\partial \theta} - \mu \\ = 0. \quad (28)$$

Furthermore, for a given  $\theta$ ,  $\mu$  can be updated iteratively by the gradient method, which is given by

$$\mu(n+1) = \left[ \mu(n) - \Delta_{\mu} \left( \frac{1}{\frac{\lg(P_{S,\max}A+1)}{\lg(P_{R,\max}B+1)} + 1} - \theta \right) \right]^+, \quad (29)$$

where  $n$  is an iteration index,  $\Delta_{\mu}$  is a positive iteration step size, and  $[a]^+$  denotes the operation  $\max(a, 0)$ . Through iteration, it is possible to get the optimal solution  $\theta_2^*$ . Note that  $\theta_1^*$  is in the feasible set of  $G_2$ , such that  $\theta^* = \theta_2^*$  is the optimal solution of the optimization problem  $J_3$ .

In summary, we propose an iteration algorithm as follows to jointly allocate source transmit power, relay transmit power,

and time ratio for the considered DF M-MIMO secure relaying system:

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**Algorithm 1** Joint Power and Time Allocation Algorithm

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- 1) Initialize the system parameters  $\alpha_{S,R}$ ,  $\alpha_{R,D}$ ,  $\alpha_{R,E}$ ,  $P_{S,\max}$ ,  $P_{R,\max}$ ,  $\varepsilon$ ,  $N_R$ ,  $\rho$ , and given a maximum tolerance  $\delta$  and a positive iteration step  $\Delta_\mu$ . Let  $n = 1$ ,  $\mu = 0$ , and  $\theta(0) = 0.5$ .
  - 2) Solve equation (28) for achieving  $\theta(n)$ .
  - 3) Update  $\mu(n)$  according to equation (29).
  - 4) If  $|R_3(\theta(n)) - R_3(\theta(n-1))| < \delta$ , then return  $\theta^* = \theta(n)$ . Otherwise, let  $n = n + 1$  and go to 2).
  - 5) Compute  $P_S^* = \min\left(P_{S,\max}, \frac{(P_{R,\max}B+1)\frac{1-\theta^*}{\theta^*}-1}{A}\right)$ , and then get  $P_R^* = \min\left(\frac{(1+P_S^*A)^{\frac{\theta^*}{1-\theta^*}}-1}{B}, P_{R,\max}\right)$ .
- 

*Remark:* Note that the solutions of these three variables  $P_S$ ,  $P_R$ , and  $\theta$  are coupled with each other. Thus, the proposed joint power and time allocation scheme can effectively improve the secrecy outage capacity compared to fixed resource allocation and separated resource allocation schemes.

#### IV. SIMULATION RESULTS

To examine the effectiveness of the proposed joint power and time allocation scheme for a DF M-MIMO secure relaying system, we present several simulation results in the following scenario: we set  $N_R = 100$ ,  $\rho = 0.9$ ,  $\varepsilon = 0.05$ , and  $P_{S,\max} = P_{R,\max} = 10$  dB, unless further specified. Additionally, for the sake of calculational simplicity, we normalize the path loss as  $\alpha_{S,R} = 1$ , and use  $\alpha_{R,D}$  and  $\alpha_{R,E}$  to denote the relative path loss. For instance,  $\alpha_{R,E} > \alpha_{R,D}$  means that the eavesdropper is closer to the relay than the legitimate destination. Note that all simulation results are obtained through Monte-Carlo simulations by averaging over 10000 channel realizations.

In simulations, we use JPTA to denote the proposed joint power and time allocation scheme. Moreover, we compare the performance of the proposed scheme with the following baseline schemes: optimal power and time allocation scheme (OPTA), degraded power and time allocation scheme (DPTA), power allocation scheme with fixed time (PAFT), time allocation scheme with fixed power (TAFP), and fixed power and time allocation scheme (FPTA). Specifically, OPTA optimally allocates transmit powers and time ratio through a three-dimensional exhaustive search, DPTA jointly optimizes source transmit power and time ratio with a fixed relay transmit power or relay transmit power and time ratio with a fixed source transmit power by maximizing the secrecy outage capacity. PAFT jointly optimizes source and relay transmit powers by maximizing the secrecy outage capacity with a fixed time ratio, TAFP optimizes the time ratio with fixed source and relay transmit powers, and FPTA adopts fixed source transmit power, relay transmit power and time ratio regardless of the system parameters.

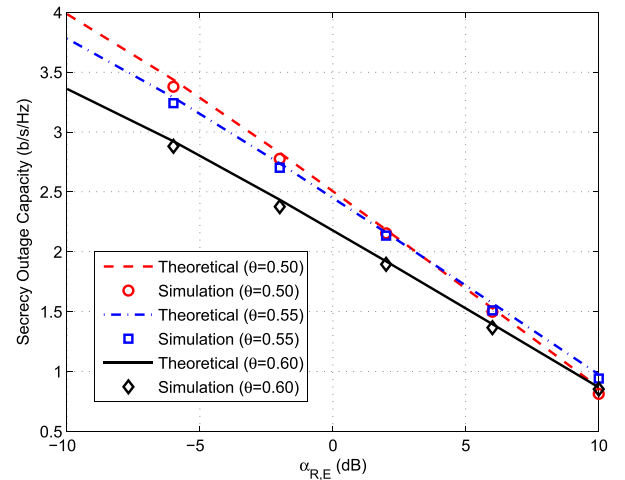


Fig. 2. Comparison of theoretical and simulation results with different values of  $\theta$ .

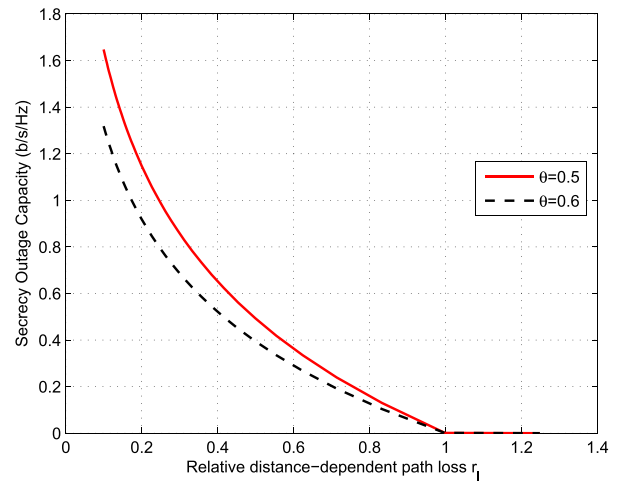


Fig. 3. The effect of relative distance-dependent path loss  $r_l$ .

First, we verify the accuracy of the derived theoretical expression of secrecy outage capacity with  $P_S = P_R = 10$  dB, and  $\alpha_{R,D} = 1.5$ . As seen in Fig. 2, the theoretical results are well consistent with the simulations in the whole  $\alpha_{R,E}$  region with different values of  $\theta$ , which proves the accuracy of the derived approximation in Theorem 1. For a given  $\theta$ , as  $\alpha_{R,E}$  increases, the secrecy outage capacity decreases accordingly. This is because the interception ability of the eavesdropper enhances when the distance between the eavesdropper and the relay becomes small. Additionally, it is found from Fig. 2 that the curve with  $\theta = 0.50$  is above the others in the small  $\alpha_{R,E}$  region, while in the large  $\theta$  region, the curve with  $\theta = 0.55$  is above the others. Thus, it is necessary to allocate the time resource between the two hops for maximizing the secrecy outage capacity.

Second, we check the effect of relative distance-dependent path loss  $r_l$  on the secrecy outage capacity with  $P_S = P_R = 10$  dB, and  $\alpha_{R,D} = 1.5$ . As claimed in the Proposition 1, only when  $0 < r_l < 1$ , the secrecy outage capacity is positive, c.f. Fig. 3. Note that all secrecy outage capacities with different values of  $\theta$  become zero from the

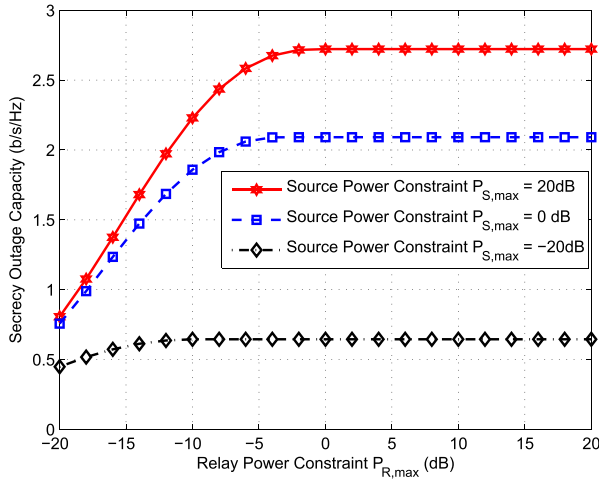


Fig. 4. The impact of source and power transmit power constraints on secrecy outage capacity for JPTA.

point of  $r_l = 1$  simultaneously, since the condition for positive secrecy outage capacity is independent of  $\theta$ . However, once  $r_l$  satisfies the condition for positive secrecy outage capacity, namely  $0 < r_l < 1$ , the positive secrecy outage capacity is a function of  $\theta$ .

Third, we show the impact of source and relay transmit power constraints on the proposed JPTA with  $\alpha_{R,E} = 1.5$ . As seen in Fig. 4, as  $P_{R,max}$  increases, the secrecy outage capacity first improves rapidly, and then saturates. This is because secrecy outage capacity is an increasing function of  $P_{R,max}$  in the region of small  $P_{R,max}$  or equivalently when  $P_{R,max} < \frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}$  according to Theorem 2. It is found that the saturated secrecy outage capacity is independent of  $P_{R,max}$  and increases with  $P_{S,max}$ , which matches with the result in Proposition 4. Moreover, the performance gain achieved by increasing  $P_{S,max}$  from 0 dB to 20 dB is obviously smaller than that by increasing  $P_{S,max}$  from -20 dB to 0 dB, since the secrecy outage capacity is saturated as  $P_{S,max}$  increases, as predicted in Proposition 3.

Next, we compare the performances of the proposed scheme JPTA and some baseline schemes, including OPTA, DPTA with  $P_S = P_{S,max}$ , DPTA with  $P_R = P_{R,max}$ , PAFT with  $\theta = 0.5$ , TAFP with  $P_S = P_{S,max}$  and  $P_R = P_{R,max}$ , and FPTA with  $P_S = P_{S,max}$ ,  $P_R = P_{R,max}$  and  $\theta = 0.5$ . In this study, we set  $\alpha_{R,D} = 3$ . As depicted in Fig. 5, JPTA always achieves the same performance as OPTA, but JPTA has a significantly lower computational complexity. Interestingly, it is found that DPTA with  $P_S = P_{S,max}$  also has the same performance as JPTA. This is because  $P_{S,max}$  is always the optimal transmit power at the source according to the proof of Theorem 3. Thus, it is likely to achieve the optimal performance with a low complexity by using DPTA with  $P_S = P_{S,max}$ . However, JPTA has a higher energy efficiency, since it may consume a lower power. Due to the same reason, DPTA with  $P_R = P_{R,max}$  is equivalent to TAFP with  $P_S = P_{S,max}$  and  $P_R = P_{R,max}$ . It is also observed that FPTA has the worst performance, since it distributes power and time resources regardless of channel conditions and

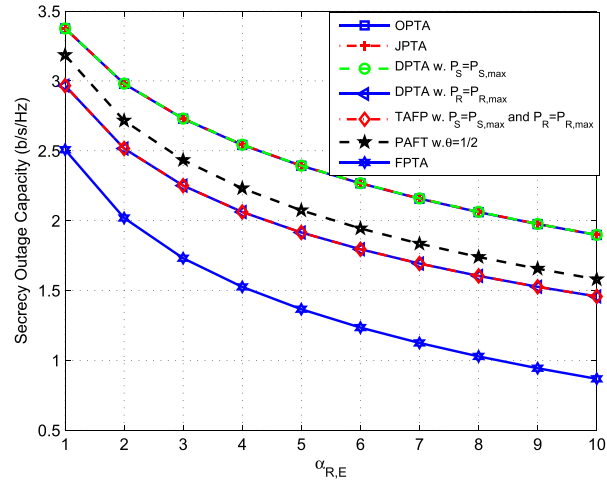


Fig. 5. Performance comparison of different resource allocation schemes.

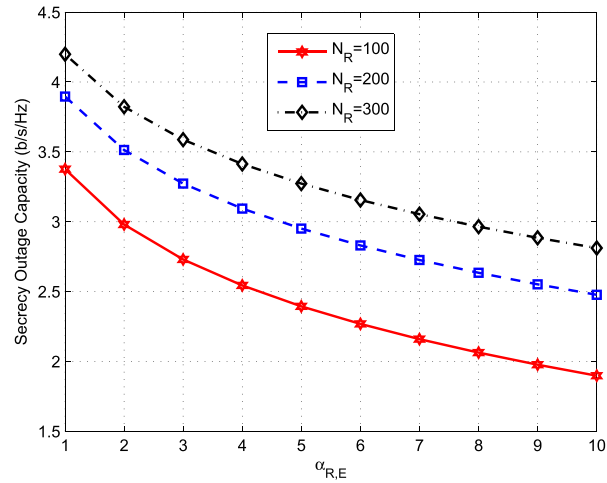


Fig. 6. Performance comparison of different numbers of relay antennas.

system parameters. In particular, compared with FPTA, JPTA achieves more performance gain as  $\alpha_{R,E}$  increases, which proves that JPTA has the capability of anti-eavesdropping of short distance.

Finally, we examine the impact of the number of antennas at the relay on the secrecy outage capacity of the proposed scheme JPTA with  $\alpha_{R,D} = 3$ . As shown in Fig. 6, with the increase of  $\alpha_{R,E}$ , all the secrecy outage capacities with different numbers of relay antennas decrease. However, for a given  $\alpha_{R,E}$ , as  $N_R$  increases, the secrecy outage capacity improves significantly. Hence, even in the case of short-distance interception, we can improve the performance to satisfy various quality of service (QoS) requirements by simply adding relay antennas, which is a main advantage of M-MIMO relaying systems.

## V. CONCLUSION

This paper provided a comprehensive performance analysis and optimization for DF M-MIMO secure relaying systems taking into account no instantaneous eavesdropper CSI and imperfect instantaneous legitimate CSI. Firstly, we derived a closed-form expression of secrecy outage capacity, revealed the condition for positive secrecy outage capacity,



and presented the requirement of the minimum number of relay antennas. Then, we proposed a joint power and time allocation scheme for maximizing the secrecy outage capacity. Afterwards, some degraded resource allocation schemes were given, which may achieve the optimal performance with a low computational complexity but a higher power consumption. Moreover, we found that the secrecy outage capacity would be saturated if maximum available source or relay power is sufficiently large.

#### APPENDIX A PROOF OF THEOREM 1

According to equation (12), the legitimate channel capacity can be computed as

$$C_D = \min(C_{S,R}, C_{R,D})$$

$$= \min \left( \theta \log_2(1 + P_S \alpha_{S,R} \|\mathbf{h}_{S,R}\|^2), (1 - \theta) \times \log_2 \left( 1 + P_R \alpha_{R,D} \left| \mathbf{h}_{R,D}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2 \right) \right) \quad (30)$$

$$= \min \left( \theta \log_2(1 + P_S \alpha_{S,R} \|\mathbf{h}_{S,R}\|^2), (1 - \theta) \times \log_2 \left( 1 + P_R \alpha_{R,D} \times \left| (\sqrt{\rho} \hat{\mathbf{h}}_{R,D}^H + \sqrt{1 - \rho} \mathbf{e}^H) \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2 \right) \right) \quad (31)$$

$$= \min \left( \theta \log_2(1 + P_S \alpha_{S,R} \|\mathbf{h}_{S,R}\|^2), (1 - \theta) \times \log_2 \left( 1 + P_R \alpha_{R,D} (\rho \|\hat{\mathbf{h}}_{R,D}\|^2 + 2\sqrt{(1 - \rho)\rho} \mathcal{R}(\mathbf{e}^H \hat{\mathbf{h}}_{R,D}) + (1 - \rho) \frac{\|\mathbf{e} \hat{\mathbf{h}}_{R,D}^H\|^2}{\|\hat{\mathbf{h}}_{R,D}\|^2} \right) \right)$$

$$\approx \min \left( \theta \log_2(1 + P_S \alpha_{S,R} \|\mathbf{h}_{S,R}\|^2), (1 - \theta) \times \log_2(1 + P_R \alpha_{R,D} \rho \|\hat{\mathbf{h}}_{R,D}\|^2) \right) \quad (32)$$

$$\approx \min \left( \theta \log_2(1 + P_S \alpha_{S,R} N_R), (1 - \theta) \times \log_2(1 + P_R \alpha_{R,D} \rho N_R) \right), \quad (33)$$

where  $\mathcal{R}(x)$  denotes the real part of  $x$ .  $\mathbf{h}_{R,D}$  is replaced with  $\sqrt{\rho} \hat{\mathbf{h}}_{R,D} + \sqrt{1 - \rho} \mathbf{e}$  in (31). Equation (32) follows from the fact that  $\rho \|\hat{\mathbf{h}}_{R,D}\|^2$  scales with the order  $\mathcal{O}(\rho N_R)$  as  $N_R \rightarrow \infty$  while  $2\sqrt{\rho(1 - \rho)} \mathcal{R}(\mathbf{e}^H \hat{\mathbf{h}}_{R,D}) + (1 - \rho) \frac{\|\mathbf{e} \hat{\mathbf{h}}_{R,D}^H\|^2}{\|\hat{\mathbf{h}}_{R,D}\|^2}$  scales with the order  $\mathcal{O}(\sqrt{N_R})$ , which is negligible. Equation (33) holds true because of  $\lim_{N_R \rightarrow \infty} \frac{\|\hat{\mathbf{h}}_{R,D}\|^2}{N_R} = 1$  and  $\lim_{N_R \rightarrow \infty} \frac{\|\mathbf{h}_{S,R}\|^2}{N_R} = 1$  according to Property A of very long random vectors in (7).

Similarly, for the eavesdropper, its channel capacity is given by

$$C_E = \min(C_{S,R}, C_{R,E})$$

$$= \min \left( \theta \log_2(1 + P_S \alpha_{S,R} N_R), (1 - \theta) \log_2 \left( 1 + P_R \alpha_{R,E} \left| \mathbf{h}_{R,E}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2 \right) \right). \quad (34)$$

Thus, according to the definition in (6), the secrecy outage probability  $\varepsilon$  with respect to a secrecy outage capacity  $C_{Soc}$  can be computed as follows:

$$\begin{aligned} \varepsilon &= P_r(C_{Soc} > C_D - C_E) \\ &= P_r(\min(C_{S,R}, C_{R,E}) > C_D - R_{Soc}) \\ &= P_r(C_{S,R} < C_{R,E}) P_r(C_{S,R} > C_D - R_{Soc}) \\ &\quad + P_r(C_{S,R} \geq C_{R,E}) P_r(C_{R,E} > C_D - R_{Soc}) \\ &= P_r \left( (1 + P_S \alpha_{S,R} N_R)^{\frac{\theta}{1-\theta}} - 1 < P_R \alpha_{R,E} \left| \mathbf{h}_{R,E}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2 \right) \\ &\quad + P_r \left( (1 + P_S \alpha_{S,R} N_R)^{\frac{\theta}{1-\theta}} - 1 \geq P_R \alpha_{R,E} \left| \mathbf{h}_{R,E}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2 \right) \\ &\quad \times P_r \left( P_R \alpha_{R,E} \left| \mathbf{h}_{R,E}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2 > 2^{(C_D - R_{Soc})/(1-\theta)} - 1 \right) \\ &= \exp \left( -\frac{(1 + P_S \alpha_{S,R} N_R)^{\frac{\theta}{1-\theta}} - 1}{P_R \alpha_{R,E}} \right) \\ &\quad + \left( 1 - \exp \left( -\frac{(1 + P_S \alpha_{S,R} N_R)^{\frac{\theta}{1-\theta}} - 1}{P_R \alpha_{R,E}} \right) \right) \\ &\quad \times \exp \left( -\frac{2^{(C_D - R_{Soc})/(1-\theta)} - 1}{P_R \alpha_{R,E}} \right) \\ &\approx \exp \left( -\frac{2^{(C_D - R_{Soc})/(1-\theta)} - 1}{P_R \alpha_{R,E}} \right), \end{aligned} \quad (35)$$

$$\approx \exp \left( -\frac{2^{(C_D - R_{Soc})/(1-\theta)} - 1}{P_R \alpha_{R,E}} \right), \quad (36)$$

where equation (35) follows the fact that  $\left| \mathbf{h}_{R,E}^H \frac{\hat{\mathbf{h}}_{R,D}}{\|\hat{\mathbf{h}}_{R,D}\|} \right|^2$  is  $\chi^2$  distributed with 2 degrees of freedom according to Property B of very long random vectors in (8), and equation (36) holds true since the term  $\exp \left( -\frac{(1 + P_S \alpha_{S,R} N_R)^{\frac{\theta}{1-\theta}} - 1}{P_R \alpha_{R,E}} \right)$  approaches zero if  $N_R$  is sufficiently large. Theorem 1 follows immediately after equation (36).

#### APPENDIX B PROOF OF PROPOSITION 1 AND THEOREM 2

To find the condition for achieving a positive secrecy outage capacity, we check the secrecy outage capacity in two cases respectively.

First, when  $P_R \geq \frac{(1 + P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}$ , the secrecy outage capacity is reduced as

$$R_{Soc}(P_R, P_S, \theta) = \theta \log_2(1 + P_S A) - (1 - \theta) \log_2(1 + P_R B r_l), \quad (37)$$

Apparently, (37) is a monotonously decreasing function of  $P_R$ , and thus the maximum secrecy outage capacity is achieved when  $P_R = \frac{(1 + P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}$ .

Then, in the case of  $P_R \leq \frac{(1 + P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}$ , the secrecy outage capacity is equivalent to

$$\begin{aligned} R_{Soc}(P_R, P_S, \theta) &= (1 - \theta) \log_2(1 + P_R A) \\ &\quad - (1 - \theta) \log_2(1 + P_R B r_l) \\ &= (1 - \theta) \log_2 \left( 1 + \frac{1 - r_l}{\frac{1}{P_R B} + r_l} \right). \end{aligned} \quad (38)$$

If  $r_l \geq 1$ ,  $C_{soc}(P_R, P_S, \theta)$  in (38) is a monotonously decreasing function of  $P_R$  when  $P_R \leq \frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}$ . Considering the monotonicity and continuity in the whole  $P_R$  region, the maximum secrecy outage capacity is 0, which is achieved at the point  $P_R = 0$ . Thus, in order to guarantee  $R_{soc}$  positive,  $r_l$  must not be equal to or greater than 1. Otherwise, if  $0 < r_l < 1$ ,  $R_{soc}(P_R, P_S, \theta)$  in (38) is a monotonously increasing function of  $P_R$  when  $P_R \leq \frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}$ . Therefore, the corresponding maximum secrecy outage capacity is obtained at the point  $P_R = \frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}$  and is positive provenly. Hence, we get the Proposition 1.

In summary, the secrecy outage capacity is an increasing function of  $P_R$  if the positive condition is satisfied, namely  $0 < r_l < 1$ . Considering the constraint on  $P_R$ , the actual optimal power at the relay is  $P_R^* = \min\left(\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}, P_{R,\max}\right)$ , where  $P_{R,\max}$  is the maximum available transmit power at the relay. Substituting  $P_R^*$  into  $R_{soc}(P_R, P_S, \theta)$ , we get the Theorem 2.

#### APPENDIX C PROOF OF THEOREM 3

We first examine the monotonicity of the objective function in  $H_2$ . It is found that when  $P_S \geq \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}$ , namely  $\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B} \geq P_{R,\max}$ , the objective function is equivalent to

$$R_1(P_S, \theta) = (1 - \theta) \log_2 \left( 1 + P_{R,\max} B \right) - (1 - \theta) \log_2 \left( 1 + P_{R,\max} B r_l \right), \quad (39)$$

where (39) holds true since the term  $\min\left(\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B}, P_{R,\max} B\right)$  in  $R_1(P_S, \theta)$  is equal to  $P_{R,\max}$  in the case of  $\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B} \geq P_{R,\max}$ . It is worth pointing out that  $R_1(P_S, \theta)$  in (39) is a constant independent of  $P_S$ .

Otherwise, if  $P_S \leq \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}$  or  $\frac{(1+P_S A)^{\frac{\theta}{1-\theta}} - 1}{B} \leq P_{R,\max}$ , the objective function is reduced as

$$R_1(P_S, \theta) = (1 - \theta) \log_2 \left( (1 + P_S A)^{\frac{\theta}{1-\theta}} \right) - (1 - \theta) \log_2 \left( 1 + ((1 + P_S A)^{\frac{\theta}{1-\theta}} - 1) r_l \right) = (1 - \theta) \log_2 \left( 1 - \frac{1 - r_l}{(1 + P_S A)^{\frac{\theta}{1-\theta}} r_l^2 + (1 - r_l) r_l} \right). \quad (40)$$

Note that  $R_1(P_S, \theta)$  in (40) monotonously increases as  $P_S$  enlarges. In this context,  $R_1(P_S, \theta)$  in (40) attains its maximum value at the point of  $P_S = \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}$ .

In conclusion,  $R_1(P_S, \theta)$  is a monotonously increasing function of  $P_S$  when  $P_S \leq \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}$ , and is a constant independent of  $P_S$  when  $P_S \geq \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}$ . Considering the constraint on the transmit power at the source,

if  $P_{S,\max} \leq \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}$ , the optimal source transmit power is  $P_{S,\max}$  or  $\min\left(P_{S,\max}, \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}\right)$ . Otherwise, the optimal source transmit power is an arbitrary value in  $\left[\frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}, P_{S,\max}\right]$ . In the sense of minimizing the energy consumption, it is better to take the value of  $\min\left(\frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}, P_{S,\max}\right)$ . Thus, the optimal source transmit power from the perspectives of both maximizing the secrecy outage capacity and minimizing the energy consumption is given by  $P_S^* = \min\left(P_{S,\max}, \frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}\right)$ .

Since  $R_1(P_S, \theta)$  is an increasing function of  $P_S$ , the maximum secrecy outage capacity in the case of  $P_S = P_S^*$  is given by  $R_2(\theta) = \min\left(R_1(P_{S,\max}, \theta), R_1\left(\frac{(P_{R,\max} B + 1)^{\frac{1-\theta}{\theta}} - 1}{A}, \theta\right)\right)$ . Thus, we get the Theorem 3.

#### APPENDIX D PROOF OF LEMMA 1

Taking the second derivative of the objective function of  $G_2$ , namely  $R_3(\theta)$ , we have

$$R_3''(\theta) = \frac{r_l(1 - r_l)(1 + P_{S,\max} A)^{\frac{\theta}{1-\theta}} (\ln(1 + P_{S,\max} A))^2}{(\theta - 1)^3 ((P_{S,\max} A)^{\frac{\theta}{1-\theta}} r_l + (1 - r_l))^2}. \quad (41)$$

Due to the fact of  $0 < \theta < 1$  and  $0 < r_l < 1$ , it is easy to verify  $R_3''(\theta) < 0$ . Thus, we get the Lemma 1.

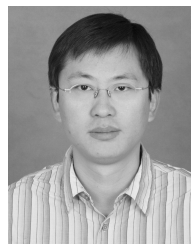
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